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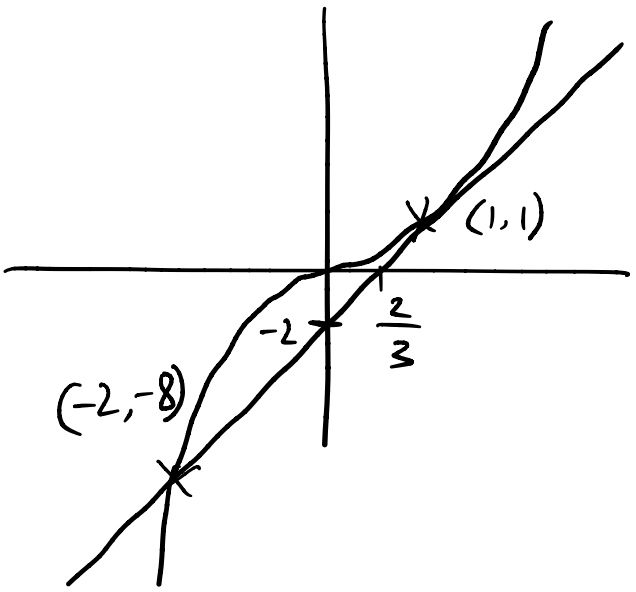

$x^3 = 3x-2$

$\Rightarrow x^3-3x+2=0$

$(x-1)(x-1)(x+2)=0$

Points of intersection: $x=-2, 1$

$3x-2=0$

$x=\frac{2}{3}$

$$\text{Area} = \int_{-2}^{1} x^3-(3x-2)\,dx$$

$$= \frac{x^4}{4}-\frac{3x^2}{2}+2x\Big|_{-2}^{1}$$

$$= \left(\frac{1}{4}-\frac{6}{4}+\frac{8}{4}\right)-\left(\frac{16}{4}-\frac{24}{4}-\frac{16}{4}\right)$$

$$= \frac{3}{4}+\frac{24}{4}$$

$$= 6\frac{3}{4}$$